

- We have that in general,  $b^{\log_b a} = a$ . Thus,  $10^{\log_{10} 9} = 9$ , and our equation becomes  $9 = 8x + 5$ , or  $x = \boxed{\text{(B)} \frac{1}{2}}$ .
- Taking 7 to the power of both sides, we have  $\log_3(\log_2 x) = 1$ . Taking 3 to the power of both sides, we have  $\log_2 x = 3$ . Finally, we have  $x = 2^3$ . Thus,  $x^{-1/2} = \frac{1}{2\sqrt{2}}$ , which is  $\boxed{\text{(E)} \text{ none of these}}$ .
- We have  $\log_2 a + \log_2 b = \log_2 ab \geq 6$ , so  $ab \geq 2^6 = 64$ . We have  $(a + b)^2 \geq 4ab$ , so  $(a + b)^2 \geq 4ab \geq 256$ . Thus,  $a + b \geq \boxed{\text{(D)} 16}$ .
- Taking the log base 10 of both sides, we have  $\log_{10} x \cdot \log_{10} x = \log_{10} 10 = 1$ , or  $(\log_{10} x)^2 = 1$ . We have  $\log_{10} x = \pm 1$ , or  $x = 10, \frac{1}{10}$ . The product of these solutions is  $\boxed{\text{(A)} 1}$ .
- We have that  $\frac{\log p}{\log 9} = \frac{\log q}{\log 12} = \frac{\log(p+q)}{\log 16}$ , or  $\frac{\log p}{2 \log 3} = \frac{\log q}{\log 3 + \log 4} = \frac{\log(p+q)}{2 \log 4}$ . Adding the first and last fraction's numerators and denominators together, we have  $\frac{\log p + \log(p+q)}{2 \log 3 + 2 \log 4} = \frac{\log q}{\log 3 + \log 4}$ . Thus,  $\log p + \log(p+q) = 2 \log q$ , or  $\log p(p+q) = \log q^2$ . Thus,  $p^2 + pq = q^2$ , and dividing by  $p^2$ , we have  $1 + \frac{q}{p} = \frac{q^2}{p^2}$ , or letting  $u = \frac{q}{p}$ ,  $1 + u = u^2$ . Using the quadratic formula, we find  $u = \frac{q}{p} = \boxed{\text{(D)} \frac{1}{2}(1 + \sqrt{5})}$ .
- Any point  $(x, y)$  on the original graph, when rotated  $90^\circ$  counterclockwise, will move to the point  $(-y, x)$ . This new graph is a function  $f$  such that  $f(-y) = x$ . But  $x = 10^y$ , so this is  $f(-y) = 10^y$ . Letting  $-y = u$ , we have  $f(u) = 10^{-u}$ , so our answer is  $\boxed{\text{(D)} y = 10^{-x}}$ .
- We have that  $\log_5(k+4) - \log_5 k = .5$ , or  $\log_5 \frac{k+4}{k} = .5$ . Taking 5 to the power of both sides, we have  $\frac{k+4}{k} = \sqrt{5}$ , or  $k+4 = \sqrt{5}k$ , which simplifies to  $k = 1 + \sqrt{5}$ . Thus, our answer is  $1 + 5 = \boxed{\text{(A)} 6}$ .
- Using the change of base log property, our equation becomes  $\frac{\log x \cdot \log x}{\log a \cdot \log b} = \frac{\log b}{\log a}$ . Since  $a, b \neq 1$ , we can multiply both sides by  $\log a \cdot \log b$  to get  $(\log x)^2 = (\log b)^2$ . Thus, we have  $\log x = \pm \log b$ , or  $x = b, \frac{1}{b}$ , giving  $\boxed{\text{(C)} 2}$  distinct values.
- Notice that  $\log_8 n = \frac{\log_2 n}{3}$  is rational only iff  $\log_2 n$  is rational, which is only true when  $n = 2^a$ . The powers of 2 from 1 to 1997 inclusive are  $1, 2, \dots, 1024$ , and taking each mod 8, we have  $0, \frac{1}{3}, \frac{2}{3}, \dots, \frac{10}{3}$ . Thus, the answer is  $\frac{1+2+\dots+10}{3} = \frac{55}{3}$ .
- This equation is equivalent to  $\frac{\log N}{\log M} = \frac{\log M}{\log N}$ , or  $(\log M)^2 = (\log N)^2$ . Since  $M, N$  are distinct, we must have  $\log M = -\log N$ , so  $\log M + \log N = 0$ , or  $MN = \boxed{\text{(B)} 1}$ .