



Math Olympiad and Problem Solving Programs

F130 - Advanced Problem Solving

Problem Set 6.1 - Addition Patterns

Name:

Date:

1.
2.
3.
4. Consider the sequence $3, 10, 17, 24, \dots, 528$. Rewrite it as additions: $3, 3 + 7, 3 + 7 + 7, 3 + 7 + 7 + 7, \dots = 3, 3 + 7, 3 + 2 \cdot 7, 3 + 3 \cdot 7, \dots, 3 + n \cdot 7$. The task is to find n . We know the last number is 528, so we can make an equation: $528 = 3 + n \times 7$. Use algebra or guess and check to solve: $525 = 7 \times n \Rightarrow n = 75$. Now we must determine the relationship between n and N . Notice the pattern. The 1st term 3 has 0 sevens, the 2nd term 10 has 1 seven, the 3rd term has 2 sevens, and so on. So the (blank) term has (blank - 1) sevens. Since 528 has 75 sevens, then it must be the 76th term. So $N =$
5.
6. Do this problem by guessing and checking. Test 5: if she has 5 quarters and 5 nickels, than she has \$1.25 in quarters and \$0.25 in nickels, and the difference between the amount in quarters and nickels is $\$1.25 - \$0.25 = \$1.00$. Keep guessing. The right answer is 9: when she has 9 quarters (or \$2.25 in quarters) and 9 nickels (or \$0.45) in nickels, the difference between the amounts is $\$2.25 - \$0.45 = \$1.80$. So we add her amounts to find the answer: $\$2.25 + \$0.45 =$
7.
8.
9.
10.