



Math Olympiad and Problem Solving Programs  
F120 - Intermediate Problem Solving  
Problem Set 4.1 - Number Patterns

Name:

Date:

1. (a)  T  
(b)  F  
(c)  F  
(d)  T  
(e)  T  
(f)  F  
(g)  T  
(h)  F  
(i)  T
2. (a)  square, triangular  
(b)  triangular  
(c)  square  
(d)  triangular
3.  24
4.  200
5.  45
6.  28, 35
7.   $1 + 2 + 3 + 4 + 5 + 6, 10 + 11$
8.  $n^{\text{th}}$  square number =  $n^{\text{th}}$  triangular number +  $(n - 1)^{\text{th}}$  triangular number. So 9th square number = 9th triangular number + 8th triangular number:   $81 = 36 + 45$
9. We have the pattern 3, 7, 11, ... We need to find the last number in this pattern less than 600. We notice that each of the numbers in our pattern is 1 less than a multiple of 4. The last multiple of 4 less than or equal to 600 is 600. So the last term in the sequence is  $600 - 1 = 599$ . So the last person the President shook hands with was 599th in line. Now we need to count how many numbers are in the pattern 3, 7, 11, ..., 599. We use our handy formula:  $(\text{last} - \text{first}) \div (\text{the number we are increasing by}) + 1$ . The last number is 599, the first number is 3, and the number we are increasing by is 4. Plug everything in:  $(599 - 3) \div 4 + 1 = 596 \div 4 + 1 = 149 + 1 =$   150
10. Subtract each corresponding number in the second lottery ticket from the first:  $22 - 12 = 10$ ,  $28 - 15 = 13$ , and so on. We notice the subtractions make a pattern: 10, 13, 16, 19, 22, 25, 28. This pattern increases by 3.