



Math Olympiad and Problem Solving Programs

E230 - Advanced Math Competitions

Grades 7 - 8

Lesson 17.2 - AMC 10 Number Theory

Name:

Date:

1. C
2. E
3. The first 2 conditions mean that the numbers must look like $4bc0, 4bc5, 5bc0, 5bc5$, 4 different numbers. So now we need to figure out how many pairs (b, c) we can have. There are 6 different pairs, $(3, 4), (3, 5), (3, 6), (4, 5), (4, 6), (5, 6)$ and for each of those 6 pairs, there are 4 different possible numbers. This gives us a total of $6 \times 4 = 24$ numbers. C
4. E
5. C
6. If the cube x is written in its prime factorization, it will look like $x = p_1^{3b_1} p_2^{3b_2} \cdots p_n^{3b_n}$ and so will have $(3b_1 + 1)(3b_2 + 1) \cdots (3b_n + 1) = 3k + 1$ for some integer k since each term of the expansion will be a multiple of 3 except for the last term which is just $1^n = 1$. In any case, we now need only find one of the answers that meets this criterion.
The answer is C since $202 = 3(67) + 1$.
7. If the bug starts on point 5, it will move to point 1. It will then move to point 2, then point 4, and back to point 1. We have a repeating pattern of $1 \rightarrow 2 \rightarrow 4$.
We just divide 1995 by 3 to use the remainder to find what point the bug finishes on. $1995 \div 3 = 665$ with no remainder so it finishes on point 4. D
8. A
9. E
10. E