



Math Olympiad and Problem Solving Programs

E230 - Advanced Math Competitions

Grades 7 - 8

Problem Set 3.1 - Counting Techniques

Name:

Date:

1.
2.
3. We want to know how we can make sets with these four different colored marbles. We can make $C(4, 1) = 4$ sets of just one marble, $C(4, 2) = 6$ sets of two marbles, $C(4, 3) = 4$ sets of 3 marbles, and $C(4, 4) = 1$ set of all four marbles. So there are $4 + 6 + 4 + 1 = \text{15}$ sets.
4. There are 9 1×1 squares, 4 2×2 squares, 1 3×3 squares, 4 $\sqrt{2} \times \sqrt{2}$ squares, and 2 $\sqrt{5} \times \sqrt{5}$ squares (one in each direction). So there are $9 + 4 + 1 + 4 + 2 = \text{20}$ squares.
5.
6. There are 2 people in the first generation, 6 people in the second, 36 in the third, and 216 in the fourth. So there are $2 + 6 + 36 + 216 = 260$ people in the family tree, and half of them is .
7.
8.
9.
10.