



1.  $\boxed{3}$  years
2.  $\boxed{\frac{1}{2}}$
3. We need to compute the sum  $-30 - 29 - 28 - \dots + 24 + 25 + 26$ . Notice that the sum  $-26 - 25 - 24 - \dots + 24 + 25 + 26 = 0$ , so all we have to calculate is  $-27 - 28 - 29 - 30 = \boxed{-114}$
4.  $\boxed{123}$
5.  $\boxed{6}$
6.  $\boxed{302}$
7.  $\boxed{24}$
8.  $\boxed{10}$
9. If a number's decimal is moved to digits to the right, it is multiplied by 100. Let  $x$  be our number. Set up an equation:  $\frac{100x-x}{11} = 21$ . Now solve:  $\frac{99x}{11} = 9x = 21$ , so  $x = \frac{21}{9} = \boxed{\frac{7}{3}}$
10.  $\boxed{6}$
11.  $\boxed{\$99}$
12.  $\boxed{12}$  dimes
13. It is more advantageous to rent 40-passenger buses, so we will rent as many as possible.  $475 \div 40 = 11R35$ . So we will have 11 40-passenger buses, which costs  $11 \times 170 = 1870$ . It is cheaper to put the last 35 students in a 40-passenger bus than two 25-passenger buses, so we will rent 12 40-passenger buses in all. It costs  $12 \times 170 = \boxed{\$2040}$  (the answer key was wrong).
14.  $11^{20,000} \approx 10^{20,000}$  which has 20,001 digits.  
 $5^{30,000} = (5^{10})^{3000} = 9,765,625^{3000} < 10,000,000^{3,000}$  which has less than 21,000 digits.  
 $2^{70,000} = (2^{10})^{7,000} = 1024^{7,000} > 1000^{7,000}$  which has more than 21,000 digits.  
Therefore  $\boxed{2^{70,000}}$  has greatest value.
15. Draw out the amounts of the jars after the first few pours.  
1st pour: Jar 1 (.5) Jar 2 (.5)  
 $\Leftarrow \frac{1}{3}$   
2nd pour: Jar 1 ( $\frac{2}{3}$ ) Jar 2 ( $\frac{1}{3}$ )  
 $\Rightarrow \frac{1}{4}$   
3rd pour: Jar 1 (.5) Jar 2 (.5)



# Math Olympiad and Problem Solving Programs

E220 - Intermediate Math Competitions

Problem Set 11.3 - MATHCOUNTS PRETEST Arithmetic

Name:

Date:

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$$\Leftarrow \frac{1}{5}$$

4th pour: Jar 1 ( $\frac{3}{5}$ ) Jar 2 ( $\frac{2}{5}$ )

$$\Rightarrow \frac{1}{6}$$

5th pour: Jar 1 (.5) Jar 2 (.5)

We notice a few patterns. On the odd numbered pours, the fractions return to half and half. On the even numbered pours, the fractions' denominators are the proportion of water moved (ex: the 4th pour moved  $\frac{1}{5}$  water, and the jars had  $\frac{3}{5}$  and  $\frac{2}{5}$ ). So we know on the 10th pour, we will move  $\frac{1}{11}$  of the water in Jar 2 to Jar 1, and by following the pattern, we find that Jar

1 will have  $\frac{6}{11}$  quarts water.