



Math Olympiad and Problem Solving Programs  
E220 - Intermediate Math Competitions  
Problem Set 11.2 - MATHCOUNTS Arithmetic

Name:

Date:

1.
2.
3. From the first bag to the fifth bag, there are four spaces between the bags. Since it is 20 feet between the first and fifth bags, there are  $20 \div 4 = 5$  feet between bags. Between the 1st and 25th bags, there are 24 spaces. Each space is 5 feet long, so the distance is  $24 \times 5 =$   feet.
4.  $24 \text{ seconds} \times 30,000 \text{ students} = 720,000 \text{ seconds total}$ .  $720,000 \text{ seconds} \div 60 \text{ seconds/min} \div 60 \text{ min/hr} = 200 \text{ hours}$  to solve the problem. So the ratio of development time to solving time is
5.
6.
7. Guess and check: 5 hours: 25 hours =  $2 \times 12 \text{ hours} + 1 \text{ hour}$ . Not the same.  
6 hours: 36 hours =  $3 \times 12 \text{ hours}$ . Not the same.  
7 hours: 49 hours =  $4 \times 12 \text{ hours} + 1 \text{ hour}$ . Not the same.  
8 hours: 64 hours =  $5 \times 12 \text{ hours} + 4 \text{ hours}$ . Not the same.  
9 hours: 81 hours =  $6 \times 12 \text{ hours} + 9 \text{ hours}$ . The same.
8.  $x + y = 15$ ,  $xy = 16$ . We want  $\frac{1}{x} + \frac{1}{y}$ . Write  $\frac{1}{x} + \frac{1}{y}$  as a single fraction with common denominator  $xy$ :  $\frac{y}{xy} + \frac{x}{xy} = \frac{x+y}{xy}$ . Since we know what  $x + y$  and  $xy$  are, we have our answer.
9. Write the numbers 1 through 15 in a line and cross out every 3rd number that is not already crossed out starting with one:  
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15  
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15  
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15  
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15  
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15  
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15  
So we end up with 3. The pattern will be the same no matter what number we start with. So if 1 is the first number we erase, 3 is the last. If 2 is the first number we erase, 4 will be last. If 3 is the first number we erase, 5 will be last, and so on. So if 11 is last, the first number erased was



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10. Keep careful track of your work. First, we find the area of the paper:  $10 \times 6 = 60$  square inches. In the notebook, there are 100 sheets, so there is a total of  $60 \times 100 = 6000$  square inches of paper in one notebook. There are 24 notebooks, so in total, there are  $24 \times 6000 = 144,000$  square inches of paper. Each square inch weighs 0.005 ounces, so the total weight of all the paper is  $144,000 \times 0.005 = 720$  ounces. The covers weigh .5 ounces per notebook, so all the notebook covers weigh  $24 \times .5 = 12$  ounces. So altogether, the notebooks weigh  $720 + 12 =$