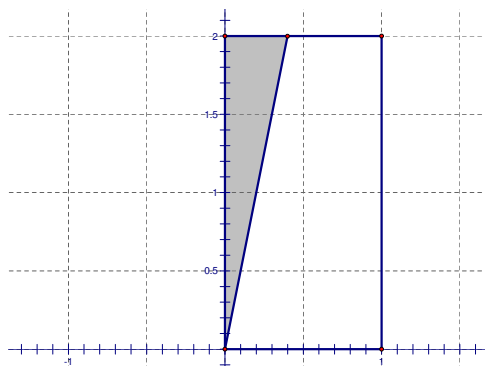
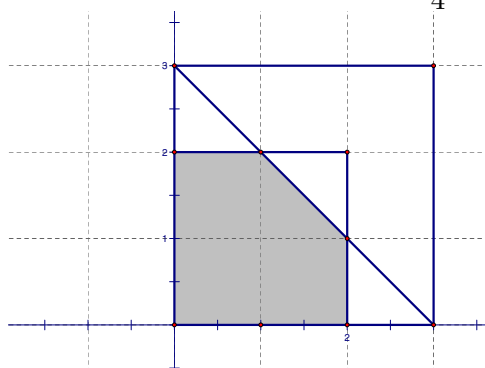


1.  $\boxed{\frac{1}{2}}$
2. The interval for which  $x^2 \leq \frac{1}{2}$  is the interval in which  $-\frac{\sqrt{2}}{2} \leq x \leq \frac{\sqrt{2}}{2}$ . This segment has length  $\sqrt{2}$ . The probability that  $x^2 \leq \frac{1}{2}$  is then  $\frac{\sqrt{2}}{2}$ . We want  $x^2 > \frac{1}{2}$ , so the answer is  $\boxed{1 - \frac{\sqrt{2}}{2}}$ .
3. First fix point  $P$ , since we're only looking at the relative position of the two points. Then  $Q$  can fall anywhere within 60 degrees left or right of  $P$ , which is an arc of 120 degrees. Therefore the probability is  $\frac{120}{360} = \boxed{\frac{1}{3}}$ .
4.  $\boxed{\frac{1}{8}}$
5.  $\boxed{\frac{1}{4}}$
6.  $\frac{y}{x} > 5$  can be written as  $y > 5x$ . Consider if it was  $y = 5x$ ; then we would have a line with slope 5.



The triangle has area  $\frac{2}{5}$ , and the rectangle has area 2, so  $\frac{\frac{2}{5}}{2} = \boxed{\frac{1}{5}}$

7. The points that lie on the perpendicular bisector  $l$  of  $(0,0)$  and  $(3,3)$  are equidistant to the two points. So all of the points below the line  $l$  are points closer to  $(0,0)$  than to  $(3,3)$ . So these are points such that  $x + y < 3$ . This is all the points inside the square except for the right triangle bordered by  $(2,1)$ ,  $(1,2)$  and  $(2,2)$ , which has area  $\frac{1}{2}$ , which means that the successful region has area  $4 - \frac{1}{2} = \frac{7}{2}$ . Thus the answer is  $\frac{\frac{7}{2}}{4} = \boxed{\frac{7}{8}}$



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8.  $\boxed{\frac{5}{12}}$

9. Since  $x, y, z$  are randomly and independently placed, any ordering for them is equally likely. There are  $3! = 6$  orderings for 3 random numbers, so the chance that it is any one particular order (in this case  $x \leq y \leq z$ ) is  $\boxed{\frac{1}{6}}$

10. Three lengths  $a, b, c$  can be the sides of the triangle if and only if they satisfy the Triangle Inequality in every possible way; that is, if  $a + b > c$ ,  $b + c > a$ , and  $c + a > b$ . Suppose that our line segment is the unit interval, and we are breaking it at points  $x$  and  $y$  with  $0 < x < y < 1$ . Then the three resulting segments will form a triangle if and only if  $x < \frac{1}{2}$ ,  $y > \frac{1}{2}$ , and  $y - x < \frac{1}{2}$ . So the "possible" region is the triangle with vertices  $(0, 0)$ ,  $(0, 1)$ ,  $(1, 1)$ , and the "successful" region is as shaded in the diagram below. Therefore the probability of success is  $\frac{\frac{1}{8}}{\frac{1}{2}} = \boxed{\frac{1}{4}}$

