



Math Olympiad and Problem Solving Programs
E210 - Introductory Math Competitions
Problem Set 26.1 - Modular Arithmetic

Name:

Date:

- all: each of 26, 32, and -4 are congruent to 2 (mod 6).
- a and c
- (a) 0 (b) 0 (c) $2010 \pmod{7} \equiv 1$. So the 2010th number in the list is the 1st in the list, or 1
- (a) $47 \equiv 2 \pmod{5}$, $742 \equiv 2 \pmod{5}$. TRUE
(b) $23 \equiv 2 \pmod{3}$, $99 \equiv 0 \pmod{3}$. FALSE
(c) $33 \equiv 0 \pmod{11}$, $333 \equiv 3 \pmod{11}$. FALSE
(d) $33 \equiv 0 \pmod{11}$, $3333 \equiv 0 \pmod{11}$. TRUE
- (a) Any odd number is $\equiv 1 \pmod{2}$. TRUE
(b) Any even number is $\equiv 0 \pmod{2}$. TRUE
(c) Any numbers that is 3 more than a multiple of 12 is $\equiv 3 \pmod{12}$. TRUE
(d) $3 \equiv 0 \pmod{3}$. $5 \equiv 2 \pmod{3}$. FALSE
(e) Any multiple of 6 is $\equiv 0 \pmod{6}$. TRUE
(f) Any multiple of 6 is divisible by 3, so it is $\equiv 0 \pmod{3}$ TRUE
(g) $3 \equiv 3 \pmod{6}$. $6 \equiv 0 \pmod{6}$. FALSE
- Numbers that are congruent to 1 (mod 9) are of the form $9k + 1$ for all integer values of k . We want these numbers to be less than or equal to 200; in other words, $9k + 1 \leq 200$. Now we solve this inequality by subtracting by 1: $9k \leq 199$, and then dividing by 9: $k \leq 22.111$. Thus, k can be any value in the list 1, 2, 3, ..., 22. So since k has 22 values, there are 22 congruent to 1 (mod 9) less than or equal to 200.
- 0, 1, 2. 3 is not a residue of mod(3), because $3 \equiv 0 \pmod{3}$.
- (a) $8 \cdot 1 + 2$ (b) $8 \cdot 3 + 4$ (c) $8 \cdot 37 + 5$ (d) $8 \cdot 299 + 0$
- (a) 2 (b) 6 (c) 2 (d) 9
- (a) 3 (b) 0 (c) 1 (d) 0