



Math Olympiad and Problem Solving Programs  
E210 - Introductory Math Competitions  
Problem Set 20.2 - Calendars

Name:

Date:

- Monday
- Tiffany takes 9 lessons a week. Divide 100 by 9 and write it out using the Division Algorithm:  $100 \div 9 = 11R1$ . So we write  $100 = 9 \times 11 + 1$ , which is *number = divisor  $\times$  quotient + remainder*. This notation is very useful to us because it shows us how to solve calendar problems easily. So Tiffany has 11 weeks of 9 lessons, with a remainder 1 lesson. So if she starts Monday, her last lesson of the complete 11 weeks of 9 lessons will be Sunday. Then her remainder 1 lesson will be Monday. But she takes 2 lessons on Monday, so the last lesson of her 100 lesson package is on Monday, and the first lesson of her second package is also Monday.
- Write 84 using the Division algorithm (see problem 2):  $84 = 6 \times 14 + 0$ . So this means Benjamin gets 14 complete weeks of 6 lessons per week. If he starts on Sunday, then the lessons will end on Friday.
- March has 31 days. If it has exactly 4 Mondays and 4 Thursdays, then the first day of the month must be Friday. This is true because if you draw out the calendar, if a month with 31 days starts on a Friday, it has 4 Mondays and 4 Thursdays, and the last day occurs on Sunday. So using math or drawing a picture of a calendar, we see that the 20th occurs on a Wednesday.
- Let there be 53 Sundays in a year. This is the maximum possible number of days that can be a single day of the week in a year. This means that January 1 starts on Sunday, and January 31 is on Tuesday. So there will be 5 Sundays in this January. Now quickly go through the rest of the months of this year and see how many months have 5 Sundays.  
Feb: Feb 1 = Wed, Feb 28 = Tues. 4 Sundays.  
Mar: Mar 1 = Wed, Mar 31 = Fri. 4 Sundays.  
Apr: Apr 1 = Sat, Apr 30 = Sun. 5 Sundays.  
May: 4 Sundays.  
June: 4 Sundays.  
July: 5 Sundays.  
Aug: 4 Sundays.  
Sept: 4 Sundays.  
Oct: 5 Sundays.  
Nov: 4 Sundays.  
Dec: 5 Sundays.  
So there are 5 months with 5 Sundays.
- Write a timeline with *DBY • Yest • Today • Tom • DAT*, where DBY = day before yesterday, and DAT = day after tomorrow. If we start with DBY and jump forward 4 days, we land on DAT. So the day after tomorrow is a Monday.
- Monday



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8.

9. A French-American will be confused when he sees a number larger than a month can be in the month spot. For instance, on February 26, 2010 which Americans write 2/26/2010, a French-American will be confused, because he is used to seeing months in the middle spot, and 26 cannot be a month. So anytime the date is 13, 14, 15, and so on, larger than 12, he will be confused.

So we need to count how many days of the week have a date number larger than 13.

In the months that have 31 days (Jan, Mar, May, Jul, Aug, Oct, Dec), the dates larger than 12 are 13, 14,  $\dots$  30, 31. There are 19 numbers in this list. So there are 7 months with 19 Confusing days, so there are  $7 \times 19 = 133$  Confusing days in these months.

In the months that have 30 days (Apr, June, Sept, Nov), the dates larger than 12 are 13, 14,  $\dots$  29, 30. There are 18 numbers in this list. So there are 4 months with 18 Confusing days, so there are  $4 \times 18 = 72$  Confusing days in these months.

In the month with 28 days (Feb), the dates larger than 12 are 13, 14,  $\dots$ , 27, 28. There are 16 numbers in this list. So there are 16 Confusing days in February.

Therefore, in total, there are  $133 + 72 + 16 = \boxed{221}$  Confusing days.

10.