

Name: \_\_\_\_\_

Date: \_\_\_\_\_

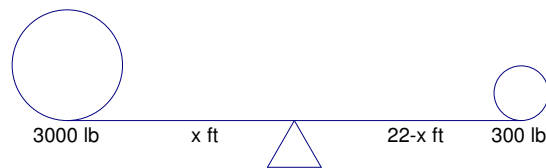
1.

2.

3.

4. The most common mistake here was to express the ratio as  $\frac{D}{34}$ . We must convert to the same units so  $D$  dollars is actually  $100D$  cents. Then the ratio is  $\frac{100D}{34} = \frac{50D}{17}$ .

5. If we let the distance from the fulcrum to the 3,000-pound weight be  $x$ , then the distance from the fulcrum to the 300-pound weight must be  $22 - x$ .



Then this gives us the following equation:

$$3000x = 300(22 - x)$$

$$3000x = 6600 - 300x$$

$$3300x = 6600$$

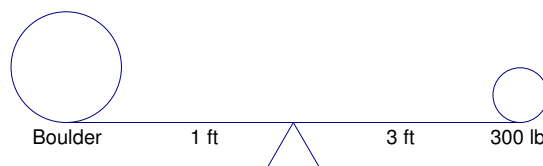
$$x = \text{2 ft from the 3,000 lb weight}$$

6.

7. If the weight of the boulder is  $x$ , then we get the following equation:

$$1x = 300 \cdot 3$$

$$x = \text{900 lb}$$



8. The common mistake was to let the ratio be  $15 : 70$ . But we have to convert the units. 70 billion = 70,000 million so our ratio is  $15 : 70,000 = \text{3 : 14,000}$ .



Math Olympiad and Problem Solving Programs  
E120 - Honors Algebra Problem Solving  
Problem Set 27.2 - Lever and Ratio

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9. We first find the rates at which Pete and his helper work. Pete completes 1 job in 6 hours or  $\frac{1}{6}$  of a job every hour. His helper can do the same job in 9 hours or  $\frac{1}{9}$  of the job in 1 hour. If they work together, they can complete  $\frac{1}{6} + \frac{1}{9} = \frac{5}{18}$  of the job in 1 hour. If they both work together to complete the job, they will take  $1 \div \frac{5}{18} = \frac{18}{5} = \boxed{3.6 \text{ hours}}$ .
10. We first find the rates at which the three pipes can fill the tank. The first two pipes fill  $\frac{1}{10}$  and  $\frac{1}{12}$  of a tank in 1 hour respectively. The third pipe can drain  $\frac{1}{15}$  of a tank in 1 hour. If all three pipes are open, the tank will be filled at a rate of  $\frac{1}{10} + \frac{1}{12} - \frac{1}{15} = \frac{7}{60}$  of the tank every hour. This means that to fill one tank, it will take  $1 \div \frac{7}{60} = \boxed{\frac{60}{7} \approx 8.57 \text{ hours}}$ .