

Name:

Date:

1.  $\boxed{34}$

2.  $\boxed{15}$

3. The even positive integers are an arithmetic sequence with  $e_1 = 2$  and a common difference of 2. This gives us  $e_n = 2 + 2(n - 1) = 2 + 2n - 2 = 2n$ . Plug in  $n = 171$  for the 171st even positive integer to be  $e_{171} = 2(171) = 342$ .

The odd positive integers are an arithmetic sequence with  $o_1 = 1$  and a common difference of 2. This gives us  $o_n = 1 + 2(n - 1) = 1 + 2n - 2 = 2n - 1$ . Plug in  $n = 219$  for the 219th odd positive integer to be  $o_{219} = 2(219) - 1 = 437$ .

The difference between the two is  $437 - 342 = \boxed{95}$ .

4. (a)  $\boxed{6, 11, 16, 21, 26; a_n = 6 + 5(n - 1) = 5n + 1}$

(b)  $\boxed{72, 66, 60, 54, 48; a_n = 72 - 6(n - 1) = 78 - 6n}$

(c)  $\boxed{0.375, 0.625, 0.875, 1.125, 1.375; a_n = 0.375 + 0.25(n - 1) = 0.25n + 0.125}$

5.  $\boxed{d = 2, a_1 = 7}$

6. (a)  $\boxed{a_1 = 5, d = 3}$

(b)  $\boxed{5, 8, 11, 14, 17}$

(c)  $\boxed{62}$

(d)  $\boxed{a_{100}}$

7. Let the two numbers be  $x, y$  with  $x < y$  and the common difference be  $d$ . Then our arithmetic sequence is  $64, x, y, 27$ .

From this we get a system of three linear equations:

$$\begin{cases} x - 64 = d \\ y - x = d \\ 27 - y = d \end{cases}$$

Solving for this system, we get  $d = -\frac{37}{3}$  and  $\boxed{(x, y) = (51\frac{2}{3}, 39\frac{1}{3})}$ .

8.  $\boxed{590}$

9.  $\boxed{23}$



Math Olympiad and Problem Solving Programs  
E120 - Honors Algebra Problem Solving  
Problem Set 26.1 - Arithmetic Sequence

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10. This is an arithmetic sequence with  $a_1 = 5100$  and  $d = 75$ . Then  $a_n = 5100 + 75(n - 1) = 5025 + 75n$ . If we let  $a_n = 7200$ , then  $n$  will be the year at which the worker will be earning the maximum salary.

$$7200 = 5025 + 75n$$

$$2175 = 75n$$

$$n = 29$$

This means in his 29th year he will be making the maximum salary so it takes the worker  years to earn this salary.