

Name:

Date:

1. $\boxed{12}$

2. $\boxed{9}$

3. Let n be the number. Then the information gives us the following equation:

$$n = 9n - 32$$

$$8n = 32$$

$$n = \boxed{4}$$

4. $\boxed{6}$

5. $\boxed{11, 13}$

6. The sides of the white box have measures $12 - x$ cm and $11 - x$ cm and area $(12 - x)\text{cm} \times (11 - x)\text{cm} = x^2 - 23x + 132\text{ cm}^2$. We know that the area of the whole box must be $11\text{ cm} \times 12\text{ cm} = 132\text{ cm}^2$. Since the area of the shaded part is 112 cm^2 , the area of the white box must be $132\text{ cm}^2 - 112\text{ cm}^2 = 20\text{ cm}^2$. This gives us the following equation:

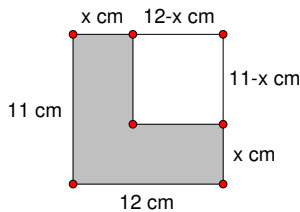
$$x^2 - 23x + 132 = 20$$

$$x^2 - 23x + 112 = 0$$

$$(x - 7)(x - 16) = 0$$

$$x = 7, 16$$

However, we know that $x < 12$ so $x = \boxed{7}$.



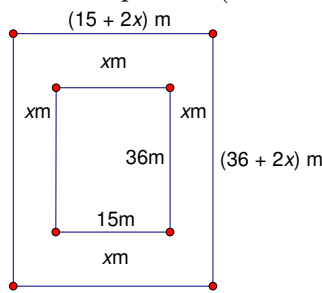
7. $\boxed{15, 17}$

8. Since the fence encloses the entire rectangle, its length, 220 m, is the perimeter of the rectangle. This tells us that, if the length and width are l, w respectively, then $l + w = 110$ or $l = 110 - w$. We also know that the area is 2800 m^2 , which tells us that $lw = 2800$. We can substitute $l = 110 - w$ into this equation to get the following:

$$\begin{aligned}(110 - w)w &= 2800 \\ 110w - w^2 &= 2800 \\ w^2 - 110w + 2800 &= 0 \\ (w - 40)(w - 70) &= 0 \\ w &= 40, 70\end{aligned}$$

This means if the width is 40 m then the length is 70 m, and if the width is 70 m then the length is 40 m. Either way the dimensions of the piece of land are $\boxed{40 \text{ m} \times 70 \text{ m}}$.

9. The lawn has an area of $36 \text{ m} \times 15 \text{ m} = 540 \text{ m}^2$. Let x be the width of the path. The width of the lawn with the path is $(15 + 2x)$ m as you can see in the picture. The length of the lawn with the path is $(36 + 2x)$ m.



This means that the area of the path must be $(15 + 2x)(36 + 2x) - 540 = 910$:

$$\begin{aligned}(15 + 2x)(36 + 2x) - 540 &= 910 \\ 540 + 102x + 4x^2 - 540 &= 910 \\ 4x^2 + 102x &= 910 \\ 4x^2 + 102x - 910 &= 0 \\ 2(2x^2 + 51x - 455) &= 0 \\ 2(2x + 65)(x - 7) &= 0 \\ x &= -\frac{65}{2}, 7\end{aligned}$$

Obviously the width of the path cannot be negative, so it must be $\boxed{7 \text{ m}}$.



Math Olympiad and Problem Solving Programs
E120 - Honors Algebra Problem Solving
Problem Set 17.2 - Quadratic Word Problems

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10. This problem may have been graded incorrectly.

Letting s, t be the speed and time of the journey respectively, $st = 120$ or $t = \frac{120}{s}$. The second piece of information gives us that $(s + 15)(t - \frac{2}{5}) = 120$. We can plug $t = \frac{120}{s}$ into the equation to get:

$$(s + 15)\left(\frac{120}{s} - \frac{2}{5}\right) = 120$$
$$120 + \frac{1800}{s} - \frac{2s}{5} - 6 = 120$$
$$\frac{1800}{s} - \frac{2s}{5} - 6 = 0$$

Multiply both sides by $5s$

$$9000 - 2s^2 - 30s = 0$$

$$s^2 + 15s - 4500 = 0$$

$$(s + 75)(s - 60) = 0$$

$$s = -75, 60$$

Obviously the car cannot be travelling at a negative speed so it must have been travelling 60 km/h.